

LGP-30 USERS' ORGANIZATION - POOL

"SEARCH FOR ROOT"

Program No. C2-37

PROGRAM DESCRIPTION

Program Title: "Search For Root"

Author: Arthur I. Larky and Jerry Rayna

Installation: Lehigh University

Purpose :

To solve for the real roots of equations of the form

$$f(x) = 0$$

by an iteration process. (The method of false position\*).

The program may be used either as a keyboard routine to print  $X$  and  $f(x)$  or as a subroutine within a program.

Input:

Two distinct initial guesses for each root must be stored in  $L_0 + 0051$  and  $L_0 + 0052$ .

A constant  $\epsilon$  stored in  $L_0 + 0062$  indicating the tolerance allowed in  $f(x)$ .

An accelerating factor may be required (optional).  
(See also Procedure).

Output:

When used as a subroutine only:  $X_0$  in the accumulator at a  $q$  determined by the subroutine used to calculate  $f(x)$ . (See below).

When used as a keyboard routine:

Decimal printout of  $X$  and  $f(x)$ . With transfer control depressed, the above is printed for each iteration. If the control button is up, printout will occur only for those values of  $f(x)$  which are less than  $\epsilon$  in absolute value.

Calling Sequence:

As a subroutine:

R $L_0 + 0110$	}	if $X_1, X_2$ and $\epsilon$ are to be inputed.
U $L_0$		
R $L_0 + 0110$	}	if $X_1, X_2$ and $\epsilon$ are already in memory
U $L_0 + 0002$		

The routine will exit with  $X_0$  in the accumulator.

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\* Hartree, "Numerical Analysis," Oxford University Press, Second Edition (1958) Page 214.

As a keyboard routine:

Transfer to  $L_0$   
 Type in  $X_1$ ,  $X_2$ , and  $\epsilon$   
 into  $L_0 + 0051$ ,  $L_0 + 0052$ , and  $L_0 + 0062$  using the  
 proper data input identification words.

Depress transfer control if every iteration is to be printed.  
 Routine will continue iteration until  $X_0$  is printed twice after which  
 an overflow stop will occur.

Subroutines Required:

1) A properly scaled subroutine capable of calculating  $f(x)$  for the  
 $X$  values most likely to be encountered must be in memory. The R-U calling  
 sequence for this subroutine must be placed into  $L_0 + 0003 - L_0 + 0004$   
 and  $L_0 + 0009 - L_0 + 0010$ .

2) A data input subroutine with calling sequence in  $L_0$  and  $L_0 + 0001$   
 (optional).

3) A data output subroutine with calling sequences in  $L_0 + 0118 - 0120$   
 and  $L_0 + 0127 - 0129$ . (optional).

4) A test quadratic  $[2x^2 + 5x + 1 = f(x)]$  is included in the coding  
 and is called by the sequence R0113, U0101 in locations 0003-4 and 0009-10.  
 $x_1$ ,  $x_2$ , and  $\epsilon$  must be entered @  $q = 4$  as usual.

Procedure:

1) The iteration uses the formula:

$$X_{i+1} = X_i - 1 + \frac{X_i - 1 - X_i}{[f(x_i) - f(x_{i-1})] / \phi} \cdot \frac{f(x_{i-1})}{\phi}$$

$$\text{where } \phi = |f(x_i)| + |f(x_{i-1})| + 1 \text{ at } 30$$

and is repeated until  $|f(x)| \leq \epsilon$

2) For use as a subroutine in a general program: The general pro-  
 gram must provide  $X_1$ ,  $X_2$ , and  $\epsilon$  in the proper memory locations or read them  
 from tape. The transfer control button may be depressed during program check-  
 out to print  $X$  and  $f(x)$  for each iteration (except the final one). Routine  
 exits with  $X_0$  in accumulator.

3) For use as a keyboard routine:

Change  $L_0 + 0027$  to U0028. Then  $X$  and  $f(x)$  will be printed  
 (at  $q$ 's determined by the data output calling sequence) when  $|f(x)| \leq \epsilon$   
 or for each iteration when the transfer control is depressed.

4) An accelerating factor to aid in convergence may be included by  
 changing  $L_0 + 0155$  to M0113. The accelerating factor (at  $q = 0$ ) should be  
 stored in  $L_0 + 0113$ . (OPTIONAL).

5) Break Points 16 and 32 should be depressed.

Programmed Stops:

Two break point 32 stops and one break point 16 stop are included. The breakpoint 32 stops follow the  $f(x)$  print and the  $X_{i+1}$  calculation. Their purpose is to permit the iteration to be halted and new values for  $X_1$ ,  $X_2$ , and  $\epsilon$  to be read in. This is done by skipping the execution of the next program step. To do so release the Break Point 32 button. When the computer stops, perform the following steps:

- a) depress One Operation button
- b) depress Manual Input button (on console)
- c) depress Start button
- d) return to Normal Operation and Start.

The break point 16 stop enables the programmer to look at the size of the correction factor for the iteration.

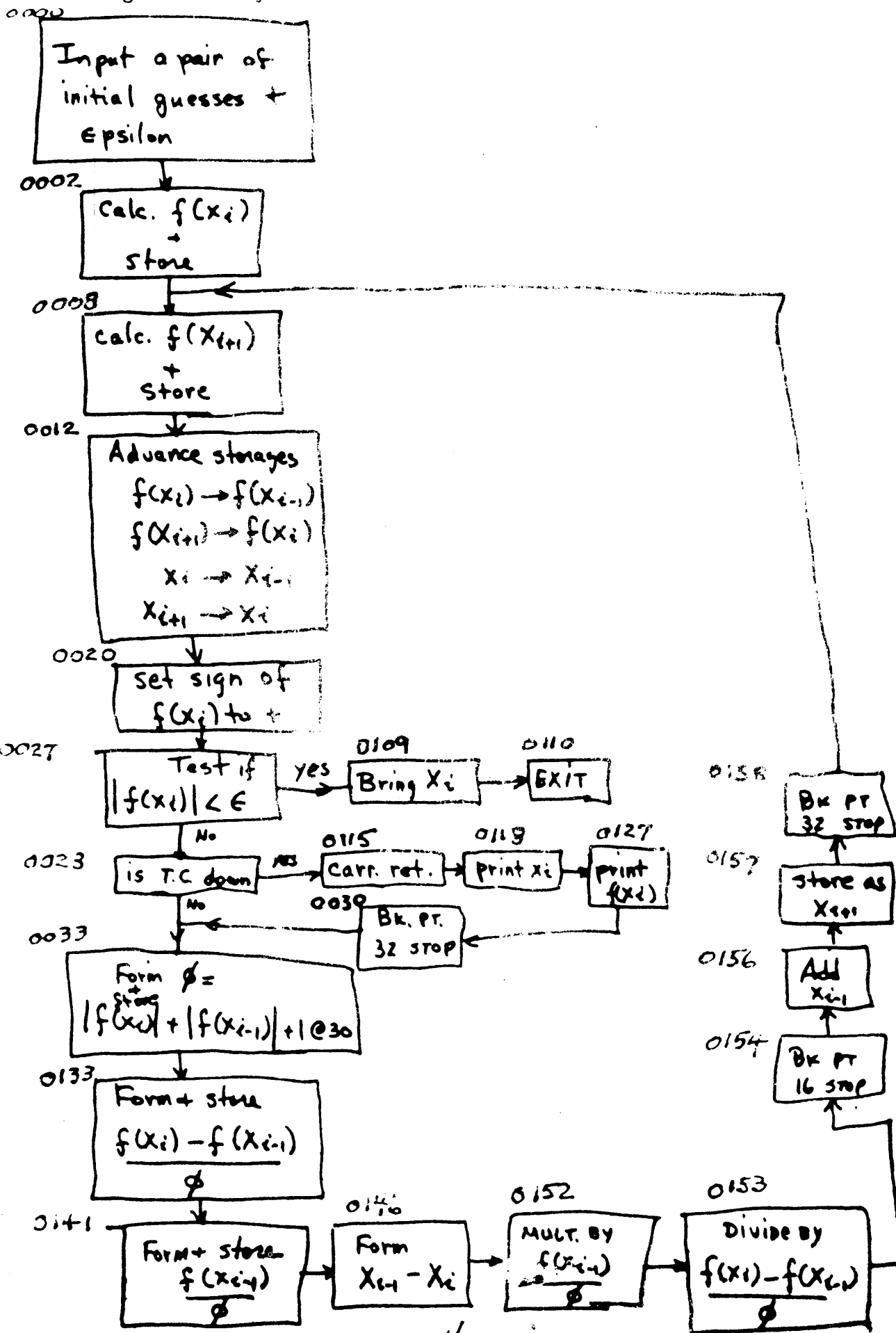
Limitations:

When used as a keyboard routine, the program will overflow stop after the second printout of the root. To search for additional roots, release the Break Point 32 button, and restart and when a break point 32 stop occurs, return to data input as outlined under Programmed Stops above.

It is likely that, if the initial guesses for  $X_1$  and  $X_2$  are too far away from  $X_0$ , overflow stops may occur. In this case merely depress the start button as often as necessary. Regardless of the presence of an overflow, some correction to  $X_i$  will be effected and ultimately values within scale will be obtained and the search continued. The function calculation subroutine must, of course, be able to handle  $X$  values reasonably near its root without overflow. The method causes looping at a point of inflection.

Storage:

127 locations, no temporary storage.



Root Search Example Problem

$$2x^2 + 5x + 1 = f(x).$$

PRM Program No. 02-4 "Search for root"  
 by A.I. Larky and G. Rayna  
 Lening University

1. With transfer control button up:

.0000800'  
 0+040851' 3' -0000003' -0000000'  
 4+040862' 1' -0000000''

Transfer to 00.

The two guesses for X.  
 The epsilon.

X	f(X)
-2.28079589	.000080
-2.28077645	.000000
-2.28077645	.000000

Final Solution.

0+040851' 0' -0000001' -0000000''

New guesses for X.

X	f(X)
-.21854294	.002807
-.21922728	-.000014
-.21922357	.000000
-.21922357	.000000

Final Solution

2. With transfer control button down:

(Note effect, if any, of depression of transfer control button on other subroutines in use; in particular, the data input routine.)

.0000800'  
 0+040851' 3' -0000003' -0000000'  
 4+040862' 1' -0000000''

Transfer to 00.

The two guesses for X.  
 The epsilon.

X	f(X)
2.999999	033.9999
-3.800000	010.8799
-7.000000	064.0000
-3.144578	005.0538
-2.814026	002.7673
-2.413957	000.5845
-2.306810	000.1086
-2.282337	000.0064
-2.280795	000.0000
-2.280776	000.0000
-2.280776	000.0000

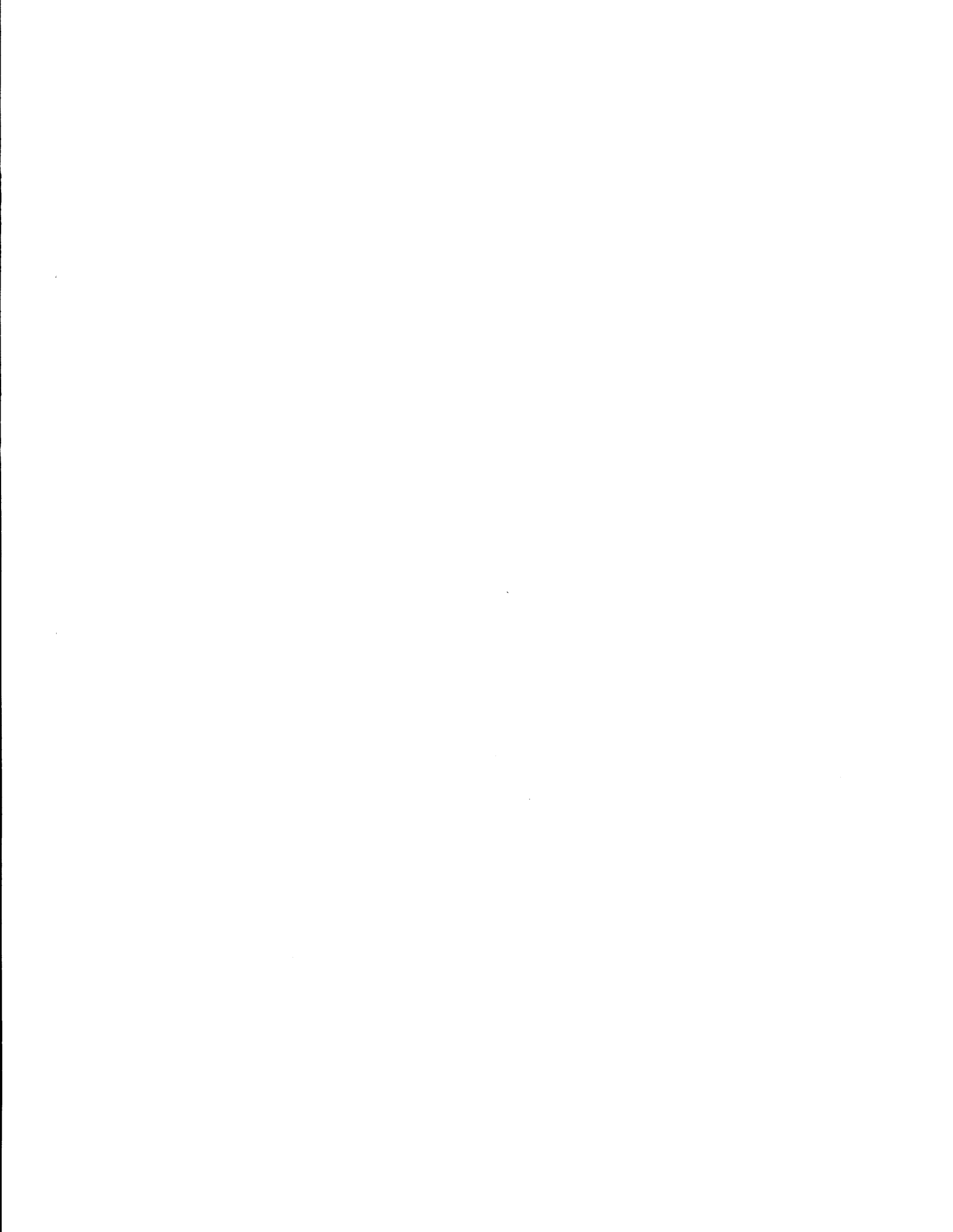
Solution after first iteration.  
 Solution after second iteration.

Final Solution

0+040851' 0' -0000001' -0000000''  
 0.000000  
 -0.333333  
 -0.230769  
 -0.218542  
 -0.219227  
 -0.219223  
 -0.219223

New guesses for X.  
 Solution after first iteration.

Final solution.



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JOB NO.	PROGRAM NO. C2-37	PROGRAM PREPARED BY: A.I. Larky and G. Rayna	PROGRAM CHECKED BY: POOL Review	DATE 2/4/60
PROBLEM: "SEARCH FOR ROOT"				TRACK

PROGRAM INPUT CODES	STOP	LOCATION	INSTRUCTION		STOP	CONTENTS OF ADDRESS	NOTES
			OPERATION	ADDRESS			
01010 L <sub>b</sub>	/						
101010 L <sub>b</sub>	/	<input checked="" type="checkbox"/>					
		01010	XIR	21710	/		Data Input Routine
		1011	XIR	21710	/		for X <sub>1</sub> , X <sub>2</sub> ∈
		1012	B	01015	/	Xi	
		1013	R	0111	/	<input checked="" type="checkbox"/>	calc. f(xi)
		1014	U	0110	/		
		1015	H	01015	/	f(xi)	
		1016	U	01010	/		
		1017			/	<input checked="" type="checkbox"/>	
		1018	B	01015	/	Xi + 1	
		1019	R	0111	/		calc. f(xi+1)
		1110	U	0110	/		
		1111	H	0106	/	<input checked="" type="checkbox"/>	f(xi+1)
		1112	B	01015	/	f(xi)	
		1113	H	01015	/		new f(xi-1)
		1114	U	01012	/		
		1115	B	01015	/	<input checked="" type="checkbox"/>	Xi+1
		1116	H	01015	/		new Xi
		1117	U	01011	/		
		1118	B	01016	/	f(xi+1)	
		1119	H	01015	/	<input checked="" type="checkbox"/>	new f(xi)
		1210	T	01114	/		change sign
		1211	U	01012	/		
		1212			/		
		1213	B	01015	/	<input checked="" type="checkbox"/>	Xi
		1214	H	01015	/		new Xi-1
		1215	U	01011	/		
		1216	S	01016	/		∈
		1217	T	01110	/	<input checked="" type="checkbox"/>	search over
		1218	810101T	01111	/		print Xi, f(xi) on but-
		1219	U	01013	/		ton
101010 0101013	/	1310			/		
		1311	<input checked="" type="checkbox"/>		/	<input checked="" type="checkbox"/>	f(xi-1) / ∅

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PROBLEM: "SEARCH FOR ROOT"			DATE: 2/4/60
			TRACK

PROGRAM INPUT CODES	STOP	LOCATION	INSTRUCTION		STOP	CONTENTS OF ADDRESS	NOTES
			OPERATION	ADDRESS			
	/						
	/	0 0 1 3 2	F	0 0 0 0 0 0	/		5 @ 6
		3 3	B	0 0 5 5	/	f(xi)	
		3 4	T	0 1 0 6	/		compl.
		3 5	U	0 0 3 6	/	X	
		3 6	H	0 0 5 8	/	f(xi)	
		3 7	B	0 0 5 6	/	f(xi-1)	
		3 8	T	0 0 4 0	/		compl.
		3 9	U	0 0 4 2	/	X	
		4 0	C	0 1 0 5	/		clear accumulator
		4 1	S	0 1 0 5 6	/	f(xi-1)	
		4 2	A	0 1 0 1 0	/	1 @ 30	
		4 3	A	0 1 0 5 8	/	X   f(xi)	
		4 4	H	0 1 2 3	/		Ø
		4 5	U	0 1 3 3	/		
1 0 1 0 1 0 0 0 1 1 9 1		4 6			/		
		4 7			/	X	
		4 8			/		
		4 9	8	0 0 0 0 0 0 0 0	/	(0106)	-1 @ 0
		5 0			/		
		5 1	[		/	X	X <sub>i+1</sub>
		5 2	[		/		X <sub>i</sub>
		5 3	[		/		X <sub>i-1</sub>
		5 4			/		
		5 5	[		/	X	f(xi)
		5 6	[		/		f(xi-1)
		5 7			/		
		5 8	[		/		f (xi)
		5 9			/	X	
		6 0			/		
		6 1	[		/		f(xi+1)
		6 2	[		/		E
		6 3			/	X	





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PROBLEM: "SEARCH FOR ROOT"				TRACK

PROGRAM INPUT CODES	STOP	LOCATION	INSTRUCTION		STOP	CONTENTS OF ADDRESS	NOTES
			OPERATION	ADDRESS			
	/						
	/	0, 1 0 1 0					1 @ 30
		10 11	H	011 511	/	x @ 4	
		10 12	M	011 214	/	2 @ 2	
		10 13	A	010 312	/	X 5 @ 6	
		10 14	U	0 1 1 1 1	/		
		10 15			/	(0040)	dump
		10 16	M	010 149	/	-1 @ 0	
		10 17	U	010 316	/	X	
		10 18			/		
		10 19	B	010 512	/	xi	
		11 10	U	010 010	/		"R" to here for search
		11 11	M	011 511	/	X @ 4	
		11 12	A	011 612	/	1 @ 10	
		11 13	U	010 010	/		
		11 14	8, 0 X F	010 010	/		-1 @ 0
		11 15	X P	1 6 1 1 1	/	X	C.R.
		11 16	B	010 512	/	xi	
		11 17	X F	010 013	/		delay
		11 18	X R	310 112	/		Data Output
		11 19	X U	310 010	/	X	
		12 10	X F	010 011	/		print xi
		12 11	U	011 216	/		
10101010101011		12 12			/		
		12 13			/	X	
		12 14	40	0 0 0 0 1 0 0	/		2 @ 2
		12 15			/		$\Delta + / \theta$
		12 16	B	010 515	/	f(xi)	
		12 17	X R	310 112	/	X	Data Output
		12 18	X U	310 010	/		
		12 19	X F	010 013	/		print f(xi)
		13 10	X F	312 611	/		Bk Pt 32 STOP
		13 11	U	010 313	/	X	

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PROBLEM: "SEARCH FOR ROOT"				TRACK

PROGRAM INPUT CODES	STOP	LOCATION	INSTRUCTION		STOP	CONTENTS OF ADDRESS	NOTES
			OPERATION	ADDRESS			
	/						
	/	X					
		0 1 3 2	U	0 1 0 1 0 1 0	/		read new X, E
		3 3	B	0 0 5 5	/	f(xi)	
		3 4	S	0 0 5 6	/	f(xi-1)	
		3 5	U	0 1 3 7	/	X	
		3 6			/		
		3 7	D	0 1 2 3	/		
		3 8	U	0 1 3 9	/		
		3 9	H	0 1 2 5	/	X	
		4 10	U	0 1 4 1	/		
		4 11	B	0 0 5 6	/	f(xi-1)	
		4 12	U	0 1 4 4	/		
		4 13			/	X	
		4 14	D	0 1 2 3	/		
		4 15	C	0 0 3 1	/		
		4 16	B	0 0 5 3	/	Xi-1	
		4 17	S	0 0 5 2	/	X Xi	
		4 18	U	0 1 5 2	/		
		4 19	M	0 1 1 4	/	-1@0	
		5 10	U	0 0 2 6	/		
		5 11			/	X	x @ 2
		5 12	M	0 0 3 1	/	f(xi-1) /	
		5 13	D	0 1 1 2 5	/		
		5 14	X F	1 6 2 6	/		Stop Bk. Pt. 16
		5 15	U	0 1 5 6	/	X	
		5 16	A	0 0 5 3	/	Xi-1	
		5 17	H	0 0 5 1	/		
		5 18	X F	3 2 3 0	/		Stop Bk. Pt. 32
		5 19	U	0 0 0 9	/	X	
		6 10	U	0 0 0 0	/		
0 1 0 1 0 1 0 1 0 1 2	/	6 11			/		
		6 12	2	0 0 0 0 0 0	/		1 @ 10
		6 13			/	X	